

## Exercises 2

### Exercise 2.1

*Radiation illuminating a sodium surface causes an electron to be emitted at a speed of 100 m/s. What is the wavelength of the incident beam?*

*(ionization energy  $E_I = 2.28 \text{ eV}$  et  $1 \text{ eV} = 1.602 \cdot 10^{-19} \text{ J}$ )*

We assume that the incident beam transmits all its energy to overcome the ionization energy and give the electron a velocity, i.e.

$$E_{\text{photon}} = E_{\text{kin}} + EI$$

By expanding, then replacing  $v$  in the equation, we find:

By developing  $E_{\text{photon}} = h\nu$  and  $E_{\text{kin}} = \frac{mv^2}{2}$ , then replacing  $v$  in the equation  $\lambda = \frac{c}{\nu}$  we find:

$$\lambda = \frac{hc}{\frac{mv^2}{2} + EI}$$

As  $1 \text{ eV} \approx 1.6 \cdot 10^{-19} \text{ J}$ , we obtain :

$$\frac{6.626 \cdot 10^{-34} \cdot 3 \cdot 10^8}{\frac{9.109 \cdot 10^{-31} \cdot 100^2}{2} + 2.28 \cdot 1.6 \cdot 10^{-19}} \text{ m} = 5.44 \cdot 10^{-7} \text{ m} = 544 \text{ nm}$$

It is therefore a green ray of light.

### Exercise 2.2

*A lamp emits energy equivalent to 7 J every second. In 10 s,  $9.4 \cdot 10^{19}$  photons are emitted. Assuming that all these photons have the same frequency, what is this frequency in PHz?*

Using the formula  $E = h\nu$ , we calculate for a photon :

$$\nu = \frac{E}{h} \cong \frac{7 \cdot 10}{6.626 \cdot 10^{-34}} \cong 1 \cdot 10^{15} \text{ Hz}$$

The frequency is therefore 1 PHz.

### Exercise 2.3

*What is the speed (in m/s) of a neutron with a wavelength of  $4.43 \cdot 10^{-1} \text{ nm}$ ? Knowing that the size of objects detected by a measurement depends on the wavelength used, give a possible application for such short wavelengths.*

Using de Broglie's relation :

$$p = mv = \frac{h}{\lambda}$$

we obtain :

$$v = \frac{h}{\lambda \cdot m_n} = \frac{6.626 \cdot 10^{-34}}{4.43 \cdot 10^{-10} \cdot 1.675 \cdot 10^{-27}} = 893 \text{ m/s}$$

Such short wavelengths can be used to detect the position of atoms within molecules. One such technique is neutron diffraction, which can be used to obtain precise molecular structures.

#### Exercise 2.4

*A photon with a wavelength of 150 pm ejects an electron from an atom with an ionization energy of  $1.12 \cdot 10^{-15} \text{ J}$ . How fast will this electron be emitted?*

We use the same equations as for Exercise 2.1:

$$v = \sqrt{\frac{2(hv - EI)}{m_E}} = \sqrt{\frac{2\left(h \cdot \frac{c}{\lambda} - EI\right)}{m_E}} = \sqrt{\frac{2\left(6.626 \cdot 10^{-34} \cdot \frac{3 \cdot 10^8}{150 \cdot 10^{-12}} - 1.12 \cdot 10^{-15}\right)}{9.109 \cdot 10^{-31}}}$$

$$= 2.12 \cdot 10^7 \text{ m/s}$$

#### Exercise 2.5

*The energy required to ionize a given atom is  $3.44 \cdot 10^{-18} \text{ J}$ . This atom absorbs a photon by emitting an electron at  $1.03 \cdot 10^6 \text{ m/s}$ .*

*What is the wavelength and type (UV, visible, infrared, gamma, ...) of the photon that was absorbed?*

Again, using the equations from Exercise 2.1, we obtain :

$$\lambda = \frac{hc}{\frac{1}{2}m_e v^2 + EI} \cong \frac{6.626 \times 10^{-34} \cdot 2 \times 10^8}{0.5 \cdot 9.109 \times 10^{-31} \cdot (1.03 \times 10^6)^2 + 3.44 \times 10^{-18}} \cong 5.07 \times 10^{-8} \text{ m}$$

With a wavelength of 50.7 nm, this is UV radiation.

#### Exercise 2.6

*What is the change in energy of a lithium atom emitting a photon with a wavelength of 683 nm? What is the color of the emitted photon?*

$$E = \frac{hc}{\lambda} \cong 2.91 \times 10^{-19} \text{ J}$$

The wavelength of 683 nm corresponds to red light.

#### Exercise 2.7

*An electron is enclosed in a space whose size is of the order of magnitude of an atom: 100 pm. What is the minimum uncertainty of its momentum?*

According to Heisenberg's inequality:

$$\Delta p \geq \frac{\hbar}{2\pi\Delta x} = \frac{h}{4\pi \cdot 10^{-10}} \cong 5.28 \times 10^{-25} \text{kg} \cdot \text{m/s}$$